

# Systematic study of breakup effects on complete fusion at energies above the Coulomb barrier

Bing Wang

Zhengzhou University & ITP

Collaborators: P. R. S. Gomes (UFF)  
En-Guang Zhao (ITP)  
Wei-Juan Zhao (ZZU)  
Shan-Gui Zhou (ITP)

PKU-CUSTIPEN Nuclear Reaction Workshop  
"Reactions and Spectroscopy of Unstable Nuclei"  
August 10-14, 2014, Peking University, Beijing

Aug. 11, 2014

# Contents

- 1 Introduction
- 2 Methods
  - The reduction method
  - The universal fusion function
- 3 Results
- 4 Summary

# Breakup and fusion

Different fusion processes can take place in collisions of weakly bound projectiles.

- Direct complete fusion (DCF)
- Sequential complete fusion (SCF)
- Incomplete fusion (ICF)
- Noncapture breakup (NCBU)

Complete fusion (CF):

SCF "+" DCF



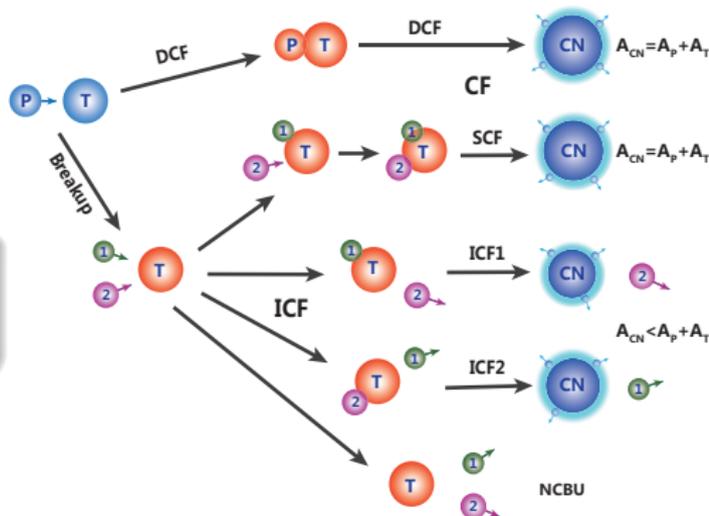
Canto et al., PR, 424, 1 (2006)



Keeley et al., PNP, 59, 579 (2007)



Back et al., RMP, 86, 317 (2014)



# The influence of breakup channel on complete fusion

- 1 Suppression on CF cross section at energies above the Coulomb barrier have been confirmed
  - Coupled channel (CC) calculation.  
[Hagino et al., PRC, 61, 037602 \(2000\)](#); [CPC, 123, 143 \(1999\)](#);  
[Marta et al., PRC, 89, 034625 \(2014\)](#)
  - Single barrier penetration model (SBPM). [Wong, PRL, 31, 766 \(1973\)](#)
- 2 Systematic behavior for the CF suppression have been investigated

- A trend of systematic behavior as a function of the target charge is not achieved.

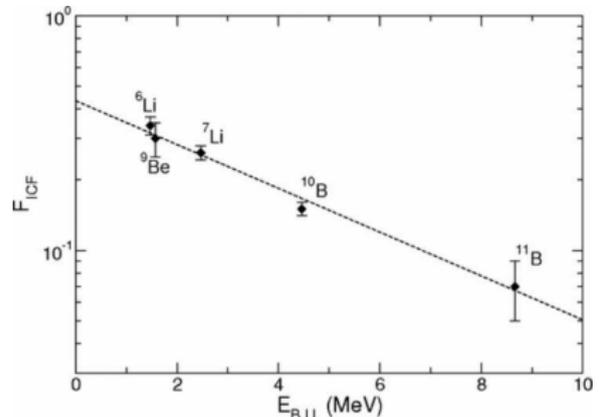
[Gomes et al. PRC, 84, 014615 \(2011\)](#)

[Sargsyan et al. PRC, 86, 054610 \(2012\)](#)

- Suppression are almost independent of the target charge for the reactions involving  ${}^6\text{Li}$ ,  ${}^7\text{Li}$ , and  ${}^{10}\text{B}$  projectiles.

[Gasques et al. PRC, 79, 034605 \(2009\)](#)

[Gasques et al. NPA, 834, 147c \(2010\)](#)



With targets of  ${}^{208}\text{Pb}$  &  ${}^{209}\text{Bi}$

[Gasques et al. PRC, 79, 034605 \(2009\)](#)

# Evidence of ICF for reactions involving tightly bound nuclei

Evidence for ICF on tightly bound nuclei have been found.

- The CF suppression factor for  $^{11}\text{B}$  on  $^{209}\text{Bi}$  is 0.93 (compared with SBPM).  
Gasques et al., PRC, 79, 034605 (2009)
- The CF cross sections have been measured for reactions involving  $^{12,13}\text{C}$  and  $^{16}\text{O}$ .  
Singh et al., PRC, 77, 014607 (2008); Kalita, JPG, 38, 095104 (2011); Yadav et al., PRC, 85, 034614 (2012)

## What we aim at?

- To explore the influence of the breakup on CF cross section at energies above the Coulomb barrier
- To perform a systematic study by comparing the fusion data with a uniform standard reference

# The reduction methods

Reduce the data for systematic study of the influence of breakup on CF.

- Eliminate completely the geometrical factors and static effects of the potential. [Canto et al. JPG, 36, 015109 \(2009\)](#); [NPA, 821, 51 \(2009\)](#)

$$E_{c.m.} \rightarrow x = \frac{E_{c.m.} - V_B}{\hbar\omega}, \quad \sigma \rightarrow F(x) = \frac{2E_{c.m.}}{R_B^2 \hbar\omega} \sigma. \quad \checkmark$$

The parameters  $R_B$ ,  $\hbar\omega$ , and  $V_B$  are obtained from the double folding and parameter-free São Paulo potential.

- No free parameters.
- Data for different reaction systems can be compared directly.

# The universal fusion function

At energies above Coulomb barrier, Wong's formula can describe the fusion cross section accurately. [Wong, PRL, 31, 766 \(1973\)](#)

$$\sigma_F^W = \frac{R_B^2 \hbar \omega}{2E_{c.m.}} \ln \left[ 1 + \exp \left( \frac{2\pi(E_{c.m.} - V_B)}{\hbar \omega} \right) \right].$$

$F(x)$  reduces to,

$$F_0(x) = \ln [1 + \exp(2\pi x)].$$

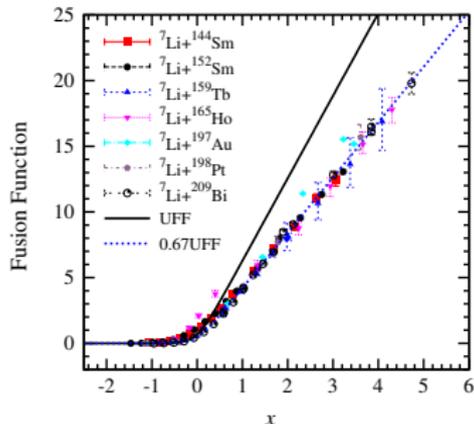
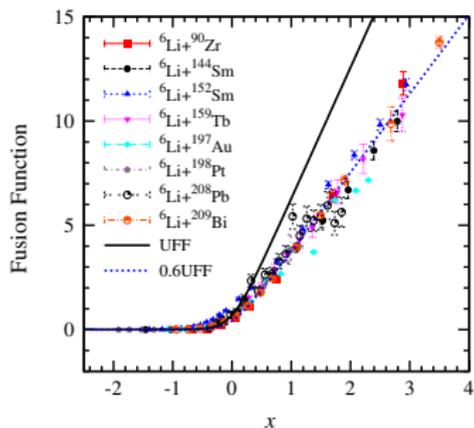
which is called the universal fusion function (UFF).



[Canto et al. JPG, 36, 015109 \(2009\); NPA, 821, 51 \(2009\)](#)

- Deviations of the fusion function,  $F(x)$ , from the UFF mainly arise from the effects of breakup on CF.

# CF functions for weakly bound nuclei ${}^6,7\text{Li}$



The breakup channel and threshold for  ${}^6\text{Li}$  is

$${}^6\text{Li} \rightarrow \alpha + d, \quad E_{\text{B.U.}} = 1.474 \text{ MeV.}$$

Suppression factor is defined as

$$F_{\text{B.U.}} = \frac{F(x)}{F_0(x)}.$$

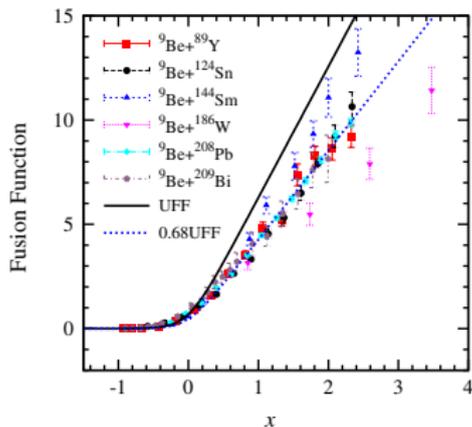
The breakup channel and threshold for  ${}^7\text{Li}$  is

$${}^7\text{Li} \rightarrow \alpha + t, \quad E_{\text{B.U.}} = 2.467 \text{ MeV.}$$

Conclusions

- The suppression is independence of the target charge.
- The suppression is stronger for  ${}^6\text{Li}$ .

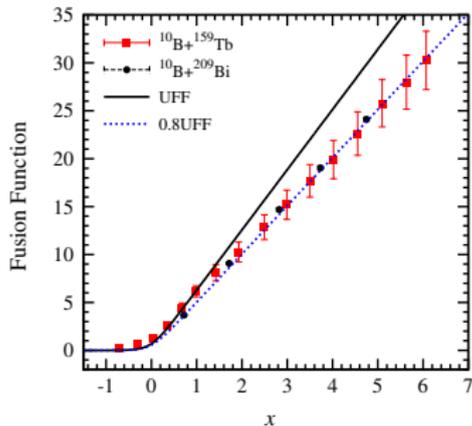
# CF functions for weakly bound nuclei $^9\text{Be}$ and $^{10}\text{B}$



- The breakup channel and threshold for  $^9\text{Be}$  is

$$^9\text{Be} \rightarrow 2\alpha + n, \quad E_{\text{B.U.}} = 1.573 \text{ MeV.}$$

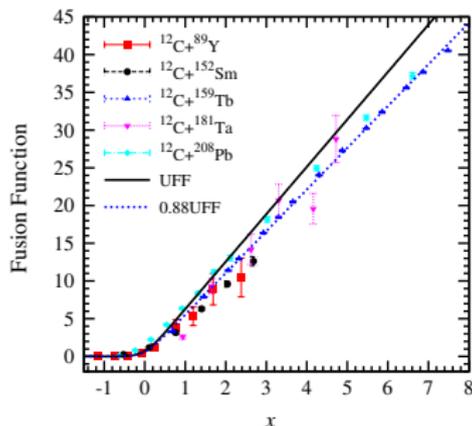
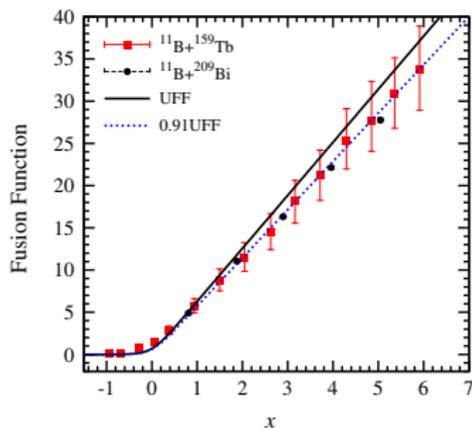
and the suppression factor is 0.68.



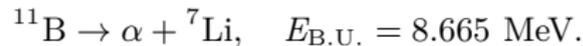
- The breakup channel and threshold for  $^{10}\text{B}$  is

$$^{10}\text{B} \rightarrow \alpha + ^6\text{Li}, \quad E_{\text{B.U.}} = 4.461 \text{ MeV.}$$

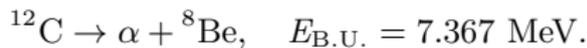
and the suppression factor is 0.8.

CF functions for tightly bound nuclei  $^{11}\text{B}$  and  $^{12}\text{C}$ 

The breakup channel and threshold for  $^{11}\text{B}$  is

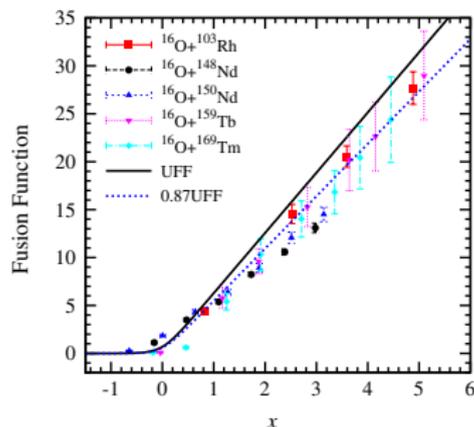
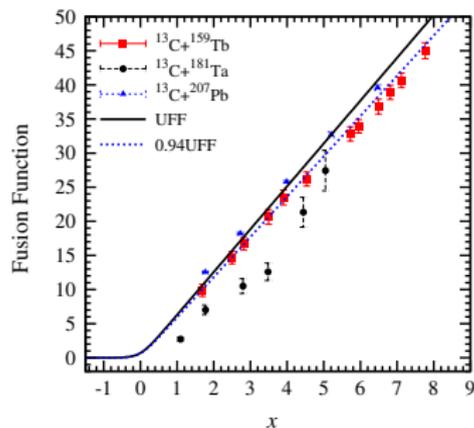


The breakup channel and threshold for  $^{12}\text{C}$  is



### Conclusions

- The suppression is confirmed.
- The  $F_{\text{B.U.}}$  are larger than that for weakly bound nuclei.
- The suppression are independence of the target charge.

CF functions for tightly bound nuclei  $^{13}\text{C}$  and  $^{16}\text{O}$ 

- The breakup channel and threshold for  $^{13}\text{C}$  is

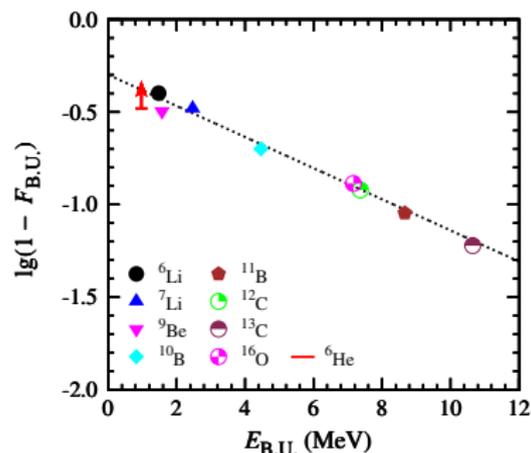
$$^{13}\text{C} \rightarrow \alpha + {}^9\text{Be}, \quad E_{\text{B.U.}} = 10.648 \text{ MeV.}$$

- The breakup channel and threshold for  $^{16}\text{O}$  is

$$^{16}\text{O} \rightarrow \alpha + {}^{12}\text{C}, \quad E_{\text{B.U.}} = 7.162 \text{ MeV.}$$

Nucleus	$E_{\text{B.U.}}$ (MeV)	$F_{\text{B.U.}}$
${}^6\text{Li}$	1.474	0.60
${}^7\text{Li}$	2.467	0.67
${}^9\text{Be}$	1.573	0.68
${}^{10}\text{B}$	4.461	0.80
${}^{16}\text{O}$	7.162	0.87
${}^{12}\text{C}$	7.367	0.88
${}^{11}\text{B}$	8.665	0.91
${}^{13}\text{C}$	10.648	0.94

# Relation between the $F_{B.U.}$ and $E_{B.U.}$



This exponential relation is given as

$$\lg(1 - F_{B.U.}) = -0.3 - 0.084E_{B.U.},$$

or equivalently,

$$\ln(1 - F_{B.U.}) = -0.69 - 0.193E_{B.U.}.$$

For halo nucleus  ${}^6\text{He}$

- The breakup channel and threshold energy is



- Suppression factor for total fusion is 0.67 (Upper limit for CF suppression).

[Canto et al. PR, \(2014\); NPA, 821, 51 \(2009\)](#)

## Conclusions

- The suppression effect of breakup on CF may indeed depend on the breakup threshold energy

[BW, Zhao, Gomes, Zhao, & Zhou. arXiv1407.5861](#)

# Summary

- ★ We perform a systematic study of the breakup effects on the complete fusion at energies above the Coulomb barrier
- ★ The reduced fusion functions are compared with the UFF and suppressed by the breakup of projectiles
  - The suppression for reaction induced by the same projectile is independence of the target charge. The suppression mainly determined by the lowest energy breakup channel of the projectile.
  - There holds a good exponential relation between the suppression factor and the energy corresponding to the lowest breakup threshold.
  - The physics behind the good exponential relation is unclear.

Thanks for your attention!

# Summary

- ★ We perform a systematic study of the breakup effects on the complete fusion at energies above the Coulomb barrier
- ★ The reduced fusion functions are compared with the UFF and suppressed by the breakup of projectiles
  - The suppression for reaction induced by the same projectile is independence of the target charge. The suppression mainly determined by the lowest energy breakup channel of the projectile.
  - There holds a good exponential relation between the suppression factor and the energy corresponding to the lowest breakup threshold.
  - The physics behind the good exponential relation is unclear.

# Thanks for your attention!